C.U.SHAH UNIVERSITY Summer Examination-2016

Subject Name : Mathematics-I

	Subject	Code : 4SC01MTC1		Branch: B. Sc.(All)			
	Semeste	r:1 Date:25/0	04/2016	Time : 10:30 To 01:30	Marks : 70		
	 Instructions: (1) Use of Programmable calculator & any other electronic instrument is prohibited. (2) Instructions written on main answer book are strictly to be obeyed. (3) Draw neat diagrams and figures (if necessary) at right places. (4) Assume suitable data if needed. 						
Q-1	a)	Attempt the followin Find the eigen values		$\begin{bmatrix} 0 & 1 \\ -1 & 2 \\ 0 & 2 \end{bmatrix}$.		(14) (02)	
	b)	Evaluate $\lim_{x\to 0} \frac{1-\cos x^2}{x^2}$	$\frac{x}{x}$.	0 21		(02)	
	c) d)	Find the center and rad	lius of the sphere lowing differentia	$x^{2} + y^{2} + z^{2} - 4x - 2y - $	6z - 11 = 0.	(02) (02)	
Atte	e) f) g) mpt any f		$x^2 + y^2 = 1$ into expansion of e^x is the theorem.	the polar form.		(02) (02) (02)	
Q-2		Attempt all questions	z			(14)	
Q-2	a)			ify it for the matrix $A = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$	$\binom{4}{3}$. Also	(07)	
	b)	State and prove Leibn	tz's theorem.			(07)	
Q-3	a)	Attempt all questions Test for consistency at 5x + 3y + 7z = 4: 3	nd solve	9; $7x + 2y + 10z = 5$.		(14) (07)	
	b)	State and prove Cauch	-	-		(07)	
Q-4	a)	Attempt all questions State standard form of $\frac{dy}{dx} - \frac{y}{x+1} = e^{3x}(x+1)$	a linear equation	of the first order and solve		(14) (07)	
	b)	Apply Gauss elimination A_{x}		-		(07)	

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 $x + 4y - z = -5; \ x + y - 6z = -12; \ 3x - y - z = 4.$

Q-5	a) b)	Attempt all questionsExpand log x in powers of $(x - 1)$ and hence evaluate log 1.1 correct to four decimal places.Find the eigen values and eigen vectors of the matrix $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$	(14) (07) (07)
Q-6	a)	Attempt all questions If $y = e^{a \sin^{-1} x}$, prove that $(1 - x^2)y_{n+2} - (2n+1)xy_{n+1} - (n^2 + a^2)y_n = 0$. Hence find the value of y_n when $x = 0$.	(14) (07)
	b)		(07)
Q-7	a)	Attempt all questions Define: rank of the matrix and find the rank of matrix $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 0 & -1 & -1 \end{bmatrix}$.	(14) (07)
	b)	$\begin{bmatrix} 0 & -1 & -1 \end{bmatrix}$ Define: Hermitian matrix. If $A = \begin{bmatrix} 2+i & 3 & -1+3i \\ -5 & i & 4-2i \end{bmatrix}$, show that AA^* is a Hermitian matrix, where A^* is conjugate transpose of A .	(07)
Q-8	a) b)	Attempt all questions Solve: $(x^2 - y^2)dx - xy dy = 0$. Reduce the matrix $A = \begin{bmatrix} -1 & 2 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$ to the diagonal form.	(14) (07) (07)

